

AP Calculus AB  
Trig Review Worksheet

Name Key

Without a calculator, evaluate each trig function at the given angle:

1.  $\cos \frac{7\pi}{6}$



$$-\frac{\sqrt{3}}{2}$$

2.  $\csc \frac{2\pi}{3}$



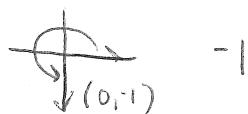
$$\frac{2\sqrt{3}}{3}$$

3.  $\tan \frac{3\pi}{4}$



$$-1$$

4.  $\sin \frac{3\pi}{2}$



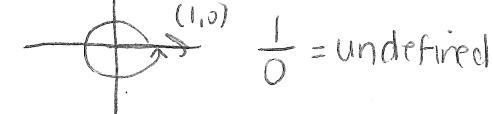
$$-1$$

5.  $\cos 240^\circ$



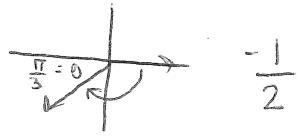
$$-\frac{1}{2}$$

6.  $\cot 2\pi$



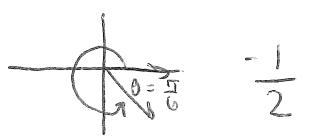
$$\frac{1}{0} = \text{undefined}$$

7.  $\cos \frac{-2\pi}{3}$



$$-\frac{1}{2}$$

8.  $\sin \frac{11\pi}{6}$



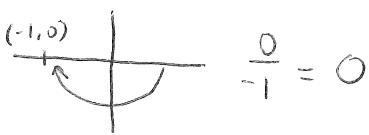
$$-\frac{1}{2}$$

9.  $\sec \frac{5\pi}{4}$



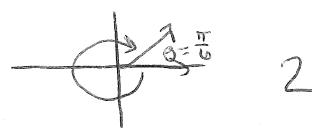
$$-\sqrt{2}$$

10.  $\tan(-\pi)$



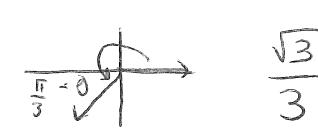
$$-\frac{0}{1} = 0$$

11.  $\csc(-330^\circ)$



$$2$$

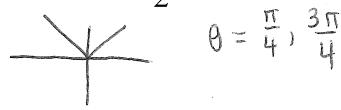
12.  $\cot \frac{4\pi}{3}$



$$\frac{\sqrt{3}}{3}$$

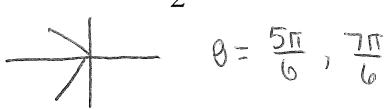
Without a calculator, solve for each angle(s) that makes the given equation true on the interval  $[0, 2\pi]$ .

13.  $\sin \theta = \frac{\sqrt{2}}{2}$



$$\theta = \frac{\pi}{4}, \frac{3\pi}{4}$$

14.  $\cos \theta = -\frac{\sqrt{3}}{2}$



$$\theta = \frac{5\pi}{6}, \frac{7\pi}{6}$$

15.  $\sec \theta = \sqrt{2}$

$$\cos \theta = \frac{\sqrt{2}}{2}$$



$$\theta = \frac{\pi}{4}, \frac{7\pi}{4}$$

16.  $\csc \theta = -1$

$$\sin \theta = -1$$



$$\theta = \frac{3\pi}{2}$$

17.  $\tan \theta = -\frac{\sqrt{3}}{3}$

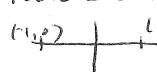
$$\cos \theta = \frac{\sqrt{3}}{2}$$



$$\theta = \frac{5\pi}{6}, \frac{11\pi}{6}$$

18.  $\cot \theta = \emptyset$

$$\tan \theta = 0$$



$$\theta = 0, \pi, 2\pi$$

Use a calculator to find each value: (round to 3 decimal places if necessary)

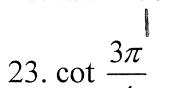
19.  $\sin 81^\circ$

$$0.988$$

22.  $\sec -270^\circ$

$$\text{undefined}$$

20.  $\tan -135^\circ$



21.  $\cos \frac{4\pi}{9}$

$$-0.174$$

23.  $\cot \frac{3\pi}{4}$

$$-1$$

24.  $\cot 90^\circ$

$$0$$

Verify each of the following identities:

$$25. \cos^3 \theta + \sin^2 \theta \cos \theta = \cos \theta$$

$$\cos \theta (\cos^2 \theta + \sin^2 \theta) = \cos \theta$$

$$\cos \theta (1) = \cos \theta$$

$$\cos \theta = \cos \theta$$

$$26. \frac{\sec^2 \theta - 1}{\tan \theta} = \tan \theta$$

$$\frac{\tan^2 \theta}{\tan \theta} = \tan \theta$$

$$\tan \theta = \tan \theta$$

$$27. (1 + \tan \theta)^2 = \sec^2 \theta + 2\tan \theta$$

$$(1 + \tan \theta)(1 + \tan \theta) = \sec^2 \theta + 2\tan \theta$$

$$1 + 2\tan \theta + \tan^2 \theta = \sec^2 \theta + 2\tan \theta$$

$$\underline{1 + 2\tan \theta + \tan^2 \theta} = \sec^2 \theta + 2\tan \theta$$

$$28. \frac{1 - 2\csc \theta}{\cot \theta} = \tan \theta - 2\sec \theta$$

$$\frac{1}{\cot \theta} - \frac{2\csc \theta}{\cot \theta} = \tan \theta - 2\sec \theta$$

$$\tan \theta - \frac{2}{\sin \theta} \cdot \frac{\sin \theta}{\cos \theta} = \tan \theta - 2\sec \theta$$

$$\tan \theta - \frac{2}{\cos \theta} = \tan \theta - 2\sec \theta$$

$$\tan \theta - 2\sec \theta = \tan \theta - 2\sec \theta$$

$$29. \csc^4 \theta - \cot^4 \theta = 2\csc^2 \theta - 1$$

$$(\csc^2 \theta + \cot^2 \theta)(\csc^2 \theta - \cot^2 \theta) = 2\csc^2 \theta - 1$$

$$(\csc^2 \theta + \cot^2 \theta)(1) = 2\csc^2 \theta - 1$$

$$\csc^2 \theta + (\csc^2 \theta - 1) = 2\csc^2 \theta - 1$$

$$2\csc^2 \theta - 1 = 2\csc^2 \theta - 1$$

$$30. \frac{1 + \sec \theta}{\tan \theta + \sin \theta} = \csc \theta$$

$$\frac{\cancel{\cos \theta}(\cos \theta + 1)}{\cancel{\cos \theta}(\sin \theta + \sin \theta \cos \theta)} = \csc \theta$$

$$\frac{\cos \theta + 1}{\sin \theta(1 + \cos \theta)} = \csc \theta$$

$$\frac{1}{\sin \theta} = \csc \theta$$

$$\csc \theta = \csc \theta$$